

**Objective:** Simplifying Radicals**Homework RX1** – NYA p.619 #1 – 12, 72, 79**Do Now: Simplify**

|              |                 |                               |
|--------------|-----------------|-------------------------------|
| 1. $2x + 5x$ | 2. $(9xy)(-4x)$ | 3. $-10y \cdot 5y^2 \cdot 3y$ |
|--------------|-----------------|-------------------------------|

**Exam Prep:** Which of the following is equivalent to  $x^6$ ?

- A)  $x^2 \cdot x^3$     B)  $x^4 \cdot x \cdot x$     C)  $x^3 + x^3$     D)  $(x^3)^3$



Yes, I'm a chicken, but I hang out with The Doctor and Abe Lincoln.

Think of simplifying radicals as a game and you will be okay.

**Exploration:** True or False

*Hint: Use perfect squares that divide evenly.*

|  |  |                     |
|--|--|---------------------|
| $\sqrt{x+y} = \sqrt{x} + \sqrt{y}$               |  | True<br>or<br>False |
| $\sqrt{xy} = \sqrt{x}\sqrt{y}$                   |  | True<br>or<br>False |
| $\sqrt{x-y} = \sqrt{x} - \sqrt{y}$               |  | True<br>or<br>False |
| $\sqrt{\frac{x}{y}} = \frac{\sqrt{x}}{\sqrt{y}}$ |  | True<br>or<br>False |

## Results

| GOOD        |  | BAD        |                                       |
|-------------|--|------------|---------------------------------------|
| <i>Mult</i> | $\sqrt{x}\sqrt{y} = \sqrt{xy}$                   | <i>Add</i> | $\sqrt{x} + \sqrt{y} \neq \sqrt{x+y}$ |
| <i>Div</i>  | $\frac{\sqrt{x}}{\sqrt{y}} = \sqrt{\frac{x}{y}}$ | <i>Sub</i> | $\sqrt{x} - \sqrt{y} \neq \sqrt{x-y}$ |

### Rules for Simplifying Radicals

A radical is simplified when both of the following are true:

- The numbers *under* the radical sign (radicands) have no square *factors*
- The number of radical signs in the expressions is as small as possible

### Hints

1. Look for *perfect square factors* in *numbers* and *variables*
2. Check your solution for simplest form using the rules

### Numbers

| Original     | Factored  | Simplified                                   |
|--------------|---|--|
| $\sqrt{24}$  | $\sqrt{4} \sqrt{6}$                                 | $2\sqrt{6}$                                  |
| $\sqrt{18}$  | $\sqrt{9} \sqrt{2}$                                 | $3\sqrt{2}$                                  |
| $\sqrt{30}$  | <b>No Perfect Square Factors</b>                    | $\sqrt{30}$                                  |
| $\sqrt{48}$  | $\sqrt{4} \sqrt{12}$ <b>Best Choice?</b>            | $2\sqrt{12}$ <b>NOT DONE</b>                 |
| $2\sqrt{12}$ | $2\sqrt{4}\sqrt{3} \rightarrow 2 \bullet 2\sqrt{3}$ | $4\sqrt{3}$                                  |
| $5\sqrt{18}$ | $5 \sqrt{9} \sqrt{2}$                               | $5 \bullet 3\sqrt{2} \rightarrow 15\sqrt{2}$ |

### Practice

|                 |                 |                  |
|-----------------|-----------------|------------------|
| 1. $\sqrt{20}$  | 2. $6\sqrt{75}$ | 3. $2\sqrt{14}$  |
| 4. $6\sqrt{16}$ | 5. $\sqrt{32}$  | 6. $10\sqrt{19}$ |

**Quick Refresh: Exponent Product Law**

$$x^3 \bullet x^7 = x^{10}$$

**Variables**

| Original    | Original        | Factored   | Simplified     |
|-------------|-----------------|--|----------------|
| <b>EVEN</b> | $\sqrt{x^6}$    | <b>Perfect ☺</b>   | $x^6$          |
| <b>EVEN</b> | $\sqrt{y^{14}}$ | <b>Perfect ☺</b>   | $y^7$          |
| <b>ODD</b>  | $\sqrt{z^9}$    | $\sqrt{z^8} \sqrt{z} \leftarrow 1^{\text{st}} \text{ Power}$ | $z^4 \sqrt{z}$ |
| <b>ODD</b>  | $\sqrt{k^{13}}$ | $\sqrt{k^{12}} \sqrt{k}$                                     | $k^6 \sqrt{k}$ |

**Practice**

|                     |                    |                    |
|---------------------|--------------------|--------------------|
| 1. $\sqrt{h^4}$     | 2. $\sqrt{x^{11}}$ | 3. $\sqrt{p^{20}}$ |
| 4. $\sqrt{c^{600}}$ | 5. $\sqrt{w^{43}}$ | 6. $\sqrt{m}$      |

### Mixed Problem

|  |                     |
|--|---------------------|
| $4\sqrt{12w^5xy^{10}z^3}$  | Original            |
| $4\sqrt{4}\sqrt{3}\sqrt{w^4}\sqrt{w}\sqrt{x}\sqrt{y^{10}}\sqrt{z^2}\sqrt{z}$ | Separate and Factor |
| $4 \cdot 2\sqrt{3} w^2\sqrt{w}\sqrt{x} y^5 z\sqrt{z}$                        | Square Root         |
| $8w^2y^5z\sqrt{3wxz}$  | Organize            |

### Mixed Practice

|                         |                              |                        |
|-------------------------|------------------------------|------------------------|
| 1. $5\sqrt{x^5y^{10}z}$ | 2. $\sqrt{100ab^7c^{20}d^8}$ | 3. $7\sqrt{18y^{10}z}$ |
|-------------------------|------------------------------|------------------------|